Research Design and Statistics

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Many thanks to Amber Trickey for sharing her slides.
Outline

• Research Design
  • Writing Research Questions
  • Study Design Overview
  • Study Design Considerations

• Statistics
  • Statistical Inference
  • Hypothesis testing
  • Statistical tests
First Step: The Research Question

- **Patient, Population or Problem**
  - Who are the relevant patients? Think about age, sex, geographic location, or specific characteristics that would be important to your question.

- **Intervention, Prognostic Factors, or Exposure**
  - What is the exposure, diagnostic test, or intervention that you are interested in?

- **Comparison**
  - What is the main alternative to compare with the intervention or exposure?

- **Outcome**
  - What can you hope to accomplish, measure, improve, or affect?
  - What are you trying to do for the patient?

- **Type of Study**
  - What would be the best study design?
Research Question Examples

• Does a multimodal analgesia (I) administered intraoperatively in general surgery patients (P) reduce self-reported pain in the 24 hours after surgery (O) compared with opioid only analgesia (C)?

• Are 30- to 50- year old men (P) who have laparoscopic hernia surgery (I) compared with those undergoing open hernia surgery (C) at increased risk for readmission to the hospital (O) during the 30 days after surgery (T)?
Study Designs

Quantitative Research Designs

Observational
  - Analytic / Hypothesis Testing
    - Cohort Study
    - Case-Control Study
  - Descriptive / Exploratory
    - Ecologic Study
    - Cross-Sectional
    - Case Series

Experimental
  - Laboratory
    - Basic Science
    - Pre-Clinical Trials
  - Human Subjects
    - Clinical Trials
    - Field Trials
    - Cluster Randomized Trials

Qualitative Research Designs

Phenomenology
Grounded Theory
Ethnography
Historical
Case Studies
Experimental vs Observational Designs

- **Experimental / Interventional**
  - Higher quality evidence
  - Investigator manipulates the conditions (i.e., Assigns treatment groups)
  - Experimental studies are only ethically permissible when “adherence to the protocol does not conflict with the subject’s best interest.”
    - Example. It is unethical to force some patients to smoke and others not to smoke

- **Non-experimental / Observational**
  - Came about due to ethical and cost restrictions of experimental studies
  - The investigator **does not assign exposure status**
  - Rely heavily on understanding the **selection of subjects** into treatment groups
    - Source of A LOT of our research design concerns.
  - **Less valid** than experimental designs but also **less resource-intensive** (time, money, data, etc.)
  - May be better for **rare outcomes**
## Analytic vs. Descriptive

<table>
<thead>
<tr>
<th>Analytic</th>
<th>Descriptive</th>
</tr>
</thead>
<tbody>
<tr>
<td>Test hypotheses</td>
<td>Generate hypotheses</td>
</tr>
<tr>
<td>Quantify the direction and magnitude of associations.</td>
<td>Identifies and describes patterns by place, time, and/or person in a population</td>
</tr>
<tr>
<td></td>
<td>Lacks a comparison group!</td>
</tr>
</tbody>
</table>
Cohort Studies

• Well-defined group of subjects that are followed over time for an outcome of interest.
• Research subjects are identified by their exposure status.
Cohort Studies

• **Prospective**
  - Exposure is assessed before the disease develops

• **Retrospective**
  - Exposure is assessed after some people have already developed disease
Cohort Studies

• **Strengths**
  • Establishes a **temporal association** between exposure and disease
  • Can measure **incidence**
  • Good for **rare exposures** and common diseases
  • Can look at **multiple outcomes**
  • Prospective studies allow better control over sampling and **better quality assessments** over time.
    • Existing data may be incomplete, inaccurate, or measured in ways that are not ideal for answering the research question.
Cohort Studies

• **Weaknesses**
  • *Recall bias* can be an issue for retrospective studies
  • *Loss-to-follow-up* can also become an issue in long prospective studies
  • Prospective cohort studies can be **resource-intensive** (large sample size, long follow-up)
  • Not good for rare diseases/outcomes
Quantitative Research Designs

Observational

- Analytic / Hypothesis Testing
  - Cohort Study
  - Ecologic Study
  - Case Series
  - Case-Control Study

- Descriptive / Exploratory
  - Cross-Sectional

Experimental

- Laboratory
  - Basic Science
  - Pre-Clinical Trials

- Human Subjects
  - Clinical Trials
  - Field Trials
  - Cluster Randomized Trials

Qualitative Research Designs

- Phenomenology
- Grounded Theory
- Ethnography
- Historical
- Case Studies
Case-Control Studies

- Research subjects are identified by their **disease status**
- **Always retrospective**
Case-Control Studies

- Key considerations
  - Case selection
    - Cases should be representative of all of diseased subjects in the community
  - Control selection
    - Controls should be similar to the cases in all respects other than the disease in question
    - Should be representative of all persons without the disease in the population from which the cases are selected
    - Should have the potential to become cases
Case-Control Studies

• **Strengths**
  • Good for *rare outcomes*
  • Can be less resource-intensive
  • Can assess *multiple exposures*
    • Case-control studies are useful for generating hypotheses about the causes of an outcome variable.

• **Weaknesses**
  • More prone to bias (recall bias, selection bias, etc.)
  • Do not estimate incidence or prevalence
  • Examine only one outcome
Cross-Sectional Studies

• Both the exposure and outcome are assessed at the same point in time or over a short period of time.
Cross-sectional Studies

**Strengths**
- Provide a point-in-time **prevalence** estimate
- Require less time to complete and **avoids the problem of loss to follow-up**
- Can be used at the beginning of a cohort or clinical trial to provide baseline characteristics

**Weaknesses**
- Does not estimate incidence
- Provides **less evidence of a causal relationship** because temporality cannot be confirmed
Ecological Studies

• Unit of analysis is a group, not the individual.
• Result in aggregate measures that are reported (descriptive) or compared (analytic).
• Also, good for rare diseases or to study the effect of large-scale public health interventions.
• Should always consider the potential ecologic fallacy
  • When the relationship observed at the group level does not represent the relationship at the individual level (ex., relationship may differ based on grouping levels)
Case Series

• Useful for:

1. Describing a **new disease** process
2. Identifying and describing **rare manifestations**
3. Identifying **emerging** health conditions

• Example. A case series of the **first 1000 patients with AIDS**. 72.7% were homosexual or bisexual males and 23.6% were injection drug users. It did not require a formal control group to conclude that these groups were at higher risk.
Case Series

• **Strengths**
  • Cost-effective method to describe rare manifestations and new/emerging diseases

• **Weaknesses**
  • Purely descriptive
  • Weakest form of evidence
  • Misleading and may suggest a plausible causal relationship where none exists in real population
Experimental Designs

• Investigator manipulates the independent variable (experimental variable)
• Better quality than observational designs
• True experimental designs involve randomization
• Quasi-experimental designs do not use randomization
  • Regression Discontinuity
  • Difference-in-Differences
  • Instrumental Variable Analysis
Randomization in Experimental Designs

- Individual randomization
  Pros: Best power per n (optimal efficiency)
  Considerations: Contamination within sites, may be infeasible

- Cluster randomization
  Pros: Minimize contamination
  Considerations: Individuals not independent, intracluster correlation coefficient (ICC), larger n needed to achieve power

- Stepped-wedge design
  Pros: All sites get intervention, random timing/order
  Considerations: Individuals not independent (ICC), much larger n needed to achieve power

[Rutterford 2015]
Hybrid Study Designs

• Combine elements of **different designs**
  • A nested case control study within a cohort study
  • A study that incorporates both a qualitative and quantitative design (Mixed Methods Study)

• Can be used to address some of issues of a single study design
## Hybrid Study Designs

<table>
<thead>
<tr>
<th>Design Concern</th>
<th>Hybrid Study Suggestion</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Underlying hypothesis</strong> is not well-supported</td>
<td>Use a qualitative design to support and guide findings in a quantitative study</td>
</tr>
<tr>
<td>Retrospective cohort data does not include <strong>detailed disease information</strong></td>
<td>Nested case-control or case-cohort to get more granular data that is not already collected</td>
</tr>
<tr>
<td>Concern about <strong>case and control selection</strong></td>
<td>Nested case-control design can ensure all cases and controls come from the same population</td>
</tr>
</tbody>
</table>
Study Design Considerations
Validity

**Internal validity**: The extent to which the observed results represent the truth in the population we are studying and, thus, are not due to methodological errors

- Study design + analysis
  - Randomized treatment assignment
  - Specific information collected (or not)
  - Data analysis methods

**External validity**: Generalizability to other settings and populations

- Study design
  - Which patients are included
  - How the treatment is implemented
Measurement Error

• **Error**: difference between the observed result and the truth
• The goal of a good research design is to **minimize error**

- Random Error
- Systematic Error
Measurement Error

• **Random Error** (Precision / Reliability)
  • The degree to which our research methods produce consistent results
  • Example. Blood pressure measurements when there is not standardized protocol
  • Exists in ALL Research Designs

• **Systematic Error** (Accuracy / Validity)
  • Closeness of a measured value to the truth
  • The degree to which we are measuring what it is supposed to measure
  • Example. Taking weights with a scale that consistently reads 5 pounds light.
Bias

• Bias is a **systematic error** in the design, conduct or analysis of a study that results in a mistaken estimate of an exposure’s effect on the risk of disease — (Schlesselman and Stolley, 1982)

• Selection bias
• Information bias
• Confounding
Selection Bias

- Method of participant selection distorts the exposure-outcome relationship from that present in the target population
  - Surveying by phone may systematically exclude patients without phones (non-response bias)
  - Patients without the exposure may be more likely to not complete the study (loss-to-follow-up bias)
  - Healthier patients may be more likely to get a certain risky treatment (confounding by indication)
  - Patients affected by the disease may be more likely to participate (volunteer bias)
Information bias

• Information bias occurs when information is collected differently between two groups (misclassification)
  
  • **Non-differential** misclassification occurs when the level of misclassification does not differ between the two groups
  • **Differential** misclassification occurs when the level of misclassification differs between the two groups

• Differential misclassification may lead to a distortion of the effect.
Confounding

• Confounding occurs when the observed result between exposure and disease differs from the truth because of the influence of the third variable.

• In contrast, effect modification is when the effect of the exposure is different among subgroups – not a distortion of the effect due to a systematic error.
Confounding

- Associated with both exposure and outcome
- Distributed *unequally* among comparison groups
- *NOT in the causal pathway* from exposure to outcome
Confounding

• Research Design Solutions
  • **Restrict** the cohort
  • **Instrumental variables**
  • **Match** comparison groups
  • **Covariate adjustment** (statistical control)
  • **Randomize** subjects (experimental design)
Statistics
Talk to a biostatistician before collecting any data!
Statistical Inference

• The process of forming judgments about the parameters of a target population using a sample drawn from that population

1. Estimation
   • Point estimation: Summarize the sample by a single value
   • Interval Estimation: Defining a range of values within which the true population parameter exists

2. Hypothesis Testing
Hypothesis Testing Steps

1. State the hypothesis
2. Identify all relevant alternative hypotheses
3. Consider the statistical assumptions
   - Variable type
   - Distributional characteristics
4. Determine the appropriate statistical test and significance level
5. Conduct the statistical test
Variable Types

Independent Variable (primary IV)
- Exposure (Intervention)
- Occurring first
- Causal relationship (?)

Dependent Variable (DV)
- Outcome
- Response variable
- Occurring after predictors

Covariate(s)
- Related to both outcome and exposure
- Must be included for internal validity
## Variable Measurement Scales

<table>
<thead>
<tr>
<th>Type of Measurement</th>
<th>Characteristics</th>
<th>Examples</th>
<th>Descriptive Stats</th>
<th>Information Content</th>
</tr>
</thead>
<tbody>
<tr>
<td>Continuous</td>
<td>Ranked spectrum; quantifiable intervals</td>
<td>Weight, BMI</td>
<td>Mean (SD) + all below</td>
<td>Highest</td>
</tr>
<tr>
<td>Ordered Discrete</td>
<td></td>
<td>Number of cigs / day</td>
<td>Mean (SD) + all below</td>
<td>High</td>
</tr>
<tr>
<td>Categorical Ordinal (Polychotomous)</td>
<td>Ordered categories</td>
<td>ASA Physical Status Classification</td>
<td>Median</td>
<td>Intermediate</td>
</tr>
<tr>
<td>Categorical Nominal (Polychotomous)</td>
<td>Unordered Categories</td>
<td>Blood Type, Facility</td>
<td>Counts, Proportions</td>
<td>Lower</td>
</tr>
<tr>
<td>Categorical Binary (Dichotomous)</td>
<td>Two categories</td>
<td>Sex (M/F), Obese (Y/N)</td>
<td>Counts, Proportions</td>
<td>Low</td>
</tr>
</tbody>
</table>

[Hulley 2007]
Variable Distributional Characteristics

(a) Negatively skewed

(b) Normal (no skew)

(c) Positively skewed

The normal curve represents a perfectly symmetrical distribution

Negative direction

Positive direction
P-values

The p-value represents the probability of finding the observed or more extreme test statistics if the null hypothesis is true.

- Measures evidence against $H_0$
- Smaller p-value, larger evidence against $H_0$
- Reject $H_0$ if p-value $\leq \alpha$
P-Value Pitfalls

• P is highly dependent on sample size

• The statistical significance ...
  - does not equal clinical significance
  - does not equal the magnitude of the effect
  ★ Report descriptive statistics with p: n1, n2, %’s, means, SD...

• P is not dichotomous yes/no, but a continuum, <0.001 to >0.99
Confidence Intervals

- Range of values within which the true population parameter exists
  - Width of the range of values is determined by a function of sample size and sample variability
- Provides more information than just the p-value alone
Determining the Statistical Test to Use
Which Statistical Test?

1. Number of IVs
2. IV Measurement Scale
3. Independent vs. Matched Groups
4. DV Measurement Scale

LEGEND:
IV = Independent Variable (i.e. predictor, exposure)
DV = Dependent Variable (i.e. response, outcome)
<table>
<thead>
<tr>
<th>OUTCOME VARIABLE</th>
<th>APPROPRIATE REGRESSION</th>
<th>MODEL COEFFICIENT</th>
</tr>
</thead>
<tbody>
<tr>
<td>Continuous AND Normal</td>
<td>Linear Regression</td>
<td>Slope ($\beta$): How much the outcome increases for every 1-unit increase in the predictor</td>
</tr>
<tr>
<td>Binary / Categorical</td>
<td>Logistic Regression</td>
<td>Odds Ratio (OR): How much the <strong>odds</strong> for the outcome increases for every 1-unit increase in the predictor</td>
</tr>
<tr>
<td>Time-to-Event</td>
<td>Cox Proportional-Hazards Regression</td>
<td>Hazard Ratio (HR): How much the <strong>rate</strong> of the outcome increases for every 1-unit increase in the predictor</td>
</tr>
</tbody>
</table>
Hierarchical / Mixed Effects Models

Correlated Data
- Grouping of subjects
- Repeated measures over time
- Multiple related outcomes

Can handle
- Missing data
- Nonuniform measures

Outcome Variable(s):
- Categorical
- Continuous
- Counts

Nested Data
## Resource

- [https://stats.idre.ucla.edu/other/dae/](https://stats.idre.ucla.edu/other/dae/)

### DATA ANALYSIS EXAMPLES

<table>
<thead>
<tr>
<th>Regression Models</th>
<th>Count Models</th>
<th>Power Analysis / Sample Size</th>
</tr>
</thead>
<tbody>
<tr>
<td>Robust Regression</td>
<td>Poisson Regression</td>
<td>Single-sample t-test</td>
</tr>
<tr>
<td>Models for Binary and Categorical Outcomes</td>
<td>Negative Binomial Regression</td>
<td>Paired-sample t-test</td>
</tr>
<tr>
<td>Logistic Regression</td>
<td>Zero-Inflated Poisson Regression</td>
<td>Independent-sample t-test</td>
</tr>
<tr>
<td>Exact Logistic Regression</td>
<td>Zero-Inflated Negative Binomial Regression</td>
<td>Two Independent Proportions</td>
</tr>
<tr>
<td>Multinomial Logistic Regression</td>
<td>Zero-Truncated Poisson</td>
<td>One-Way ANOVA</td>
</tr>
<tr>
<td>Ordinal Logistic Regression</td>
<td>Zero-Truncated Negative Binomial</td>
<td>Multiple Regression</td>
</tr>
<tr>
<td>Probit Regression</td>
<td>Censored and Truncated Regression</td>
<td>Accuracy in Parameter Estimation</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Analysis Tools</th>
<th>Stata</th>
<th>SAS</th>
<th>SPSS</th>
<th>Mplus</th>
<th>R</th>
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</thead>
<tbody>
<tr>
<td>Robust Regression</td>
<td>Yes</td>
<td>Yes</td>
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<td>Models for Binary and Categorical Outcomes</td>
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<td>Yes</td>
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<tr>
<td>Multinomial Logistic Regression</td>
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<td>Yes</td>
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<td>Yes</td>
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<td>Ordinal Logistic Regression</td>
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<td>Yes</td>
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<td>Poisson Regression</td>
<td>Yes</td>
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<tr>
<td>Negative Binomial Regression</td>
<td>Yes</td>
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<td>Yes</td>
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<tr>
<td>Zero-Inflated Poisson Regression</td>
<td>Yes</td>
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<td>Zero-Inflated Negative Binomial Regression</td>
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<tr>
<td>Zero-Truncated Poisson</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
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<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Censored and Truncated Regression</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
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<tr>
<td>Tobit Regression</td>
<td>Yes</td>
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<td>Yes</td>
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<tr>
<td>Truncated Regression</td>
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<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Interval Regression</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
</tbody>
</table>
Thanks! Questions?

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“We are all apprentices in a craft where no one ever becomes a master.” —Ernest Hemingway
Seven Habits of Highly Effective Data Users

1. **Check quality before quantity.** All data are not created equal; good statistics cannot salvage biased data.

2. **Describe before you analyze.** Special data require special tests; improper analysis gives deceptive results.

3. **Accept the uncertainty of all data.** All observations have some random error; interpretation requires estimating precision or confidence.

4. **Measure error with the right statistical test.** Positive results should be qualified by the chance of being wrong, negative results should be qualified by chance of having missed a true effect.

5. **Put clinical importance before statistical significance.** Statistical tests measure error, not importance; an appropriate measure of clinical importance must be checked.

6. **Seek the sample source.** Results from one dataset do not necessarily apply to others.

7. **View science as a cumulative process.** A single study is rarely definitive.

[Rosenfeld 2014]
Chi-Square or Fisher’s Exact (if any cell N<10)

**Outcome Variable:**
- Binary

**Predictor Variable(s):**
- Categorical
- Independent groups
- 2+ groups
- 1 independent variable

### 2 x 2 Table:

<table>
<thead>
<tr>
<th>Predictor</th>
<th>Outcome</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>MI +</td>
</tr>
<tr>
<td>GA</td>
<td>324</td>
</tr>
<tr>
<td>RA</td>
<td>20</td>
</tr>
<tr>
<td>Tot</td>
<td>344</td>
</tr>
</tbody>
</table>
Student’s T-test

Outcome Variable:
- Continuous
- Normally distributed

Predictor Variable(s):
- 1 Categorical IV
- 2 Independent groups
Analysis of Variance (ANOVA)

Outcome Variable:
- Continuous
- Normally distributed

Predictor Variable(s):
- 1 Categorical IV
- 3+ Independent groups
Paired T-test

Outcome Variable:
- Continuous
- Normally distributed

Predictor Variable(s):
- 1 Categorical IV
- 2 matched / dependent groups

1st vs. 2nd CEA Operative Time
**Outcome Variable:**
- Continuous

**Predictor Variable(s):**
- 1 Continuous IV
- Normally distributed

**Pearson’s Correlation**

CEA Op Time by BMI

Operative Time (Minutes)

BMI
Linear Regression

Outcome Variable:
- Continuous

Predictor Variable(s):
- Categorical OR continuous
- Number of IVs
  - 1 = simple linear regression
  - 2+ = multiple linear regression

CEA Op Time by BMI
Logistic Regression

Outcome Variable:
- Dichotomous (binary)

Predictor Variable(s):
- Categorical OR continuous
- Number of IVs
  - 1 = simple logistic regression
  - 2+ = multiple logistic regression
P-values

\[ n_i = 2 \left( \frac{Z_{1-\alpha/2} + Z_{1-\beta}}{\text{Effect Size}} \right)^2 \]

<table>
<thead>
<tr>
<th>The null hypothesis was</th>
<th>Null hypothesis is</th>
<th>TRUE</th>
<th>FALSE</th>
</tr>
</thead>
<tbody>
<tr>
<td>rejected ((P &lt; \alpha))</td>
<td>\textbf{Type I error}, false positive probability = (\alpha)</td>
<td>(\times)</td>
<td>true positive probability = (1 - \beta) (\textit{power of the test})</td>
</tr>
<tr>
<td>not rejected ((P \geq \alpha))</td>
<td>true negative probability = (1 - \alpha)</td>
<td>(\checkmark)</td>
<td>\textbf{Type II error}, false negative probability = (\beta)</td>
</tr>
</tbody>
</table>
References


