

# Impact of Residual Gradient Moments on Diffusion Weighted Imaging

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## Synopsis

**Bulk motion corrupts diffusion measurements in the heart but can be mitigated by nulling first and second gradient moments. When using optimization methods to design diffusion gradient waveforms with moment nulling, imperfect gradient waveforms arise from discrete convergence criteria, which impart residual (non-zero) gradient moments. This leads to intravoxel dephasing, signal loss, and inaccurate ADC measurements. Herein, simulations show that residual  $M_0 \leq 10^{-2} \text{mT/m}\cdot\text{s}$ ,  $M_1 \leq 10^{-4} \text{mT/m}\cdot\text{s}^2$ , and  $M_2 \leq 10^{-5} \text{mT/m}\cdot\text{s}^3$  leads to  $\leq 5\%$  increase in ADC. This work defines convergence criteria requirements for residual gradient moments that enable faster optimizations and more accurate measurements of ADC when using optimization methods for cardiac DWI sequence design.**

## Introduction

Diffusion-weighted imaging (DWI) measurements provide clinical value, but sensitivity to bulk motion frequently contributes to signal losses that can confound diffusion measurements, especially in moving tissues like the heart. Bulk motion sensitivity can be mitigated by using velocity ( $M_1=0$ ) and/or acceleration-compensated ( $M_1=M_2=0$ ) gradient waveforms to null the intravoxel phase dispersion from the bulk (coherent) motion of spins while preserving the intravoxel phase dispersion from incoherent diffusing spins. When using optimization methods to design diffusion gradient waveforms with moment nulling, imperfect gradient waveforms arise from discrete convergence criteria, which impart residual (non-zero) gradient moments. This leads to intravoxel dephasing, signal loss, and inaccurate ADC measurements. The intrinsic symmetry of conventional diffusion encoding strategies ensure exactly zero residual gradient moments as the waveforms are equal and opposite on either side of the refocusing pulse. However, optimization methods, which generate asymmetric gradient waveforms<sup>1-5</sup>, are increasingly used for time optimal gradient waveform design and/or to add additional constraints that mitigate bulk motion, eddy currents, and concomitant field terms. In designing an optimization scheme, it is important to identify optimization criteria that enable fast solutions to be obtained. If convergence criteria are unnecessarily strict, then convergence times can be unacceptably long (i.e. minutes), whereas real-time (i.e. less than 10-50ms) solve times are preferred. The purpose of this work was to define acceptable limits for residual gradient moments that confer  $\leq 5\%$  measurement bias for ADC in the presence of bulk motion.

## Methods

Numerical simulations were performed in Matlab to analyze the impact of residual gradient moments on intravoxel phase dispersion. The measured ADC was calculated for each of the 10,000 simulated spins per voxel as  $ADC' = \frac{1}{-b} \ln \left[ abs \left( \sum_{n=1}^{10,000} \frac{S_{DWI}^n}{S_0} \right) \right]$ , for  $b=1000 \text{mm}^2/\text{s}$ ,  $ADC=3 \times 10^{-3} \text{mm}^2/\text{s}$ , and  $S_0=10,000$ , representing the cumulative signal within the voxel in the absence of diffusion encoding gradients and intravoxel phase dispersion. The diffusion weighted signal for the  $n^{\text{th}}$  spin was calculated as  $S_{DWI}^n = e^{-bADC} e^{-i\phi_n}$ , with  $\phi_n = \gamma r_n M_0 + \gamma v_n M_1 + \gamma a_n M_2$ ,  $\gamma$  as the gyromagnetic ratio,  $r_n$ ,  $v_n$ , and  $a_n$  as the simulated position, velocity and acceleration of the  $n^{\text{th}}$  spin, and  $M_0$ ,  $M_1$  and  $M_2$  as the zero, first, and second order residual gradient moments. To analyze the impact of residual  $M_0$ ,  $ADC'$  was computed for different pixel sizes (1-10mm) with residual values of  $M_0$  and  $M_1=M_2=0$ . To analyze the impact of residual  $M_1$ ,  $ADC'$  was computed for simulated intravoxel velocity gradients, of varying maximum velocities (0-0.2m/s), with residual values of  $M_1$  and  $M_0=M_2=0$ . To analyze the impact of residual  $M_2$ ,  $ADC'$  was computed for simulated intravoxel acceleration gradients, of varying maximum accelerations (0-1m/s<sup>2</sup>), with residual values of  $M_2$  and  $M_0=M_1=0$ . The following residual gradient moments were used in the simulations: 0,  $10^{-6}$ ,  $10^{-5}$ ,  $10^{-4}$ ,  $10^{-3}$ ,  $10^{-2}$ ,  $10^{-1}$ ,  $10^0$ , and 10 with units of  $\text{mT/m}\cdot\text{s}$  for  $M_0$ ,  $\text{mT/m}\cdot\text{s}^2$  for  $M_1$  and  $\text{mT/m}\cdot\text{s}^3$  for  $M_2$ .

## Results

The impact of residual gradient moments on the measured ADC is shown in Figure 1 as a function of residual  $M_0$  and pixel size (Figure 1A), residual  $M_1$  and intravoxel velocity gradients (Figure 1B) and residual  $M_2$  and intravoxel acceleration gradients (Figure 1C).

## Discussion

Achieving precise gradient moment nulling is difficult. The simulations in this work show that knowledge of the pixel size and expected tissue motion can help define acceptable residual moment nulling thresholds while maintaining ADC measurements within 5%. The degree of intravoxel signal dephasing depends on the product of intravoxel velocity and acceleration gradients and any residual gradient moment(s). Residual  $M_0$  will always lead to an increase in the measured ADC due to intravoxel signal dephasing. A negligible ( $\leq 5\%$ ) increase in the measured ADC is observed when the residual  $M_0$  is on the order of  $10^{-2} \text{mT/m}\cdot\text{s}$  for all simulated pixel sizes (0-10mm) and  $10^{-1} \text{mT/m}\cdot\text{s}$  for simulated pixel sizes  $\leq 4.5 \text{mm}$ . Hence, higher resolution imaging is less prone to bulk motion artifacts. Residual  $M_1$  and  $M_2$  similarly lead to an increase in the measured ADC. A negligible ( $\leq 5\%$ ) increase in the measured ADC is observed when the residual  $M_1$  is on the order of  $10^{-4} \text{mT/m}\cdot\text{s}^2$  or when the residual  $M_2$  is on the order of  $10^{-5} \text{mT/m}\cdot\text{s}^3$ . Defining acceptable thresholds for residual gradient moments is important when using convex optimized diffusion encoding gradient design approaches, where the residual moments need to be specified as a constraint in the optimization. Setting these values to a specific non-zero, but nearly zero value ensures minimal signal dephasing while also providing shorter optimization convergence times.

## Conclusion

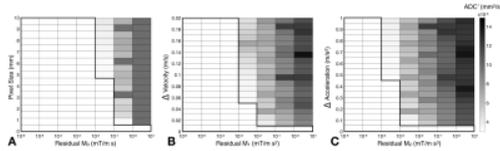
Residual gradient moments can lead to an increase in the measured ADC in DWI due to intravoxel signal dephasing. This work helps to define acceptable thresholds for residual gradient moments, which can be used to enable fast and more accurate measurements of ADC when using optimization methods for the pulse sequence design of diffusion sequences.

## Acknowledgements

## References

1. Aliotta et al. Convex optimized diffusion encoding (CODE) gradient waveforms for minimum echo time and bulk motion compensated diffusion weighted MRI. *Magn Reson Med* 2017;77:717–729.
2. Aliotta et al. Eddy current-nulled Convex Optimized Diffusion Encoding (EN-CODE) for distortion-free diffusion tensor imaging with short echo times. *Magn Reson Med* 2018;79:663–672.
3. Yang et al. Eddy current nulled constrained optimization of isotropic diffusion encoding gradient waveforms. *Magn Reson Med* 2018;00:1–15.
4. Sjölund et al. Constrained optimization of gradient waveforms for generalized diffusion encoding. *J Magn Reson* 2015;261:157–168.
5. Loecher et al. Accelerating 4D-Flow Acquisitions by Reducing TE and TR with Optimized RF and Gradient Waveforms. *ISMRM 2018*

## Figures



**Figure 1:** Numerical simulations showing the impact on the measured ADC ( $ADC'$ ) arising from intravoxel phase dispersion (signal loss) as a function of residual  $M_0$  and pixel size (**A**), residual  $M_1$  and intravoxel velocity gradients (**B**), and residual  $M_2$  and intravoxel acceleration gradients (**C**). Measured  $ADC'$  values that vary  $\leq 5\%$  compared to the simulated ADC ( $3 \times 10^{-3} \text{mm}^2/\text{s}$ ) and b-value ( $1000 \text{mm}^2/\text{s}$ ), are highlighted by the black borders (lower-left area within plots).